



Department of Medical Physics

UNIVERSITY OF WISCONSIN - MADISON
SCHOOL OF MEDICINE AND PUBLIC HEALTH

RED

RADIOLOGICAL ENGINEERING
& DESIGN LABORATORY

Implications of Heterogenous Dose Distributions for Radiopharmaceutical Therapy Revisited

Bryan P. Bednarz

Associate Professor
Department of Medical Physics
Wisconsin Institute for Medical Research
University of Wisconsin – Madison

CIRMS, Gaithersburg, MD

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Disclosures

I'm the co-founder and CSO of Voximetry, LCC a Middleton-based nuclear medicine dosimetry company.

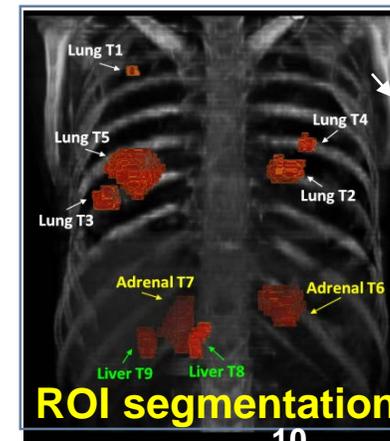
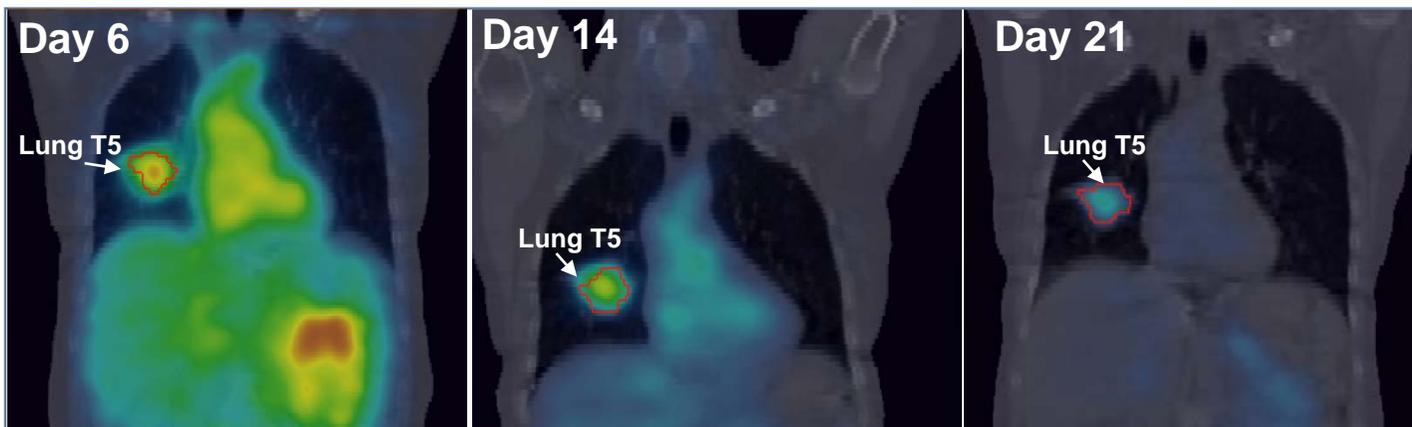


Background

- When radiopharmaceutical therapy fails to produce significant improvement in local control it is primarily due to:

Patient-specific dosimetry can help!

- Tumor selectivity
- Limited radiation tolerance of normal tissues
- Tumor radiosensitivity
- Heterogeneous uptake within the tumor (i.e. heterogeneous dose)



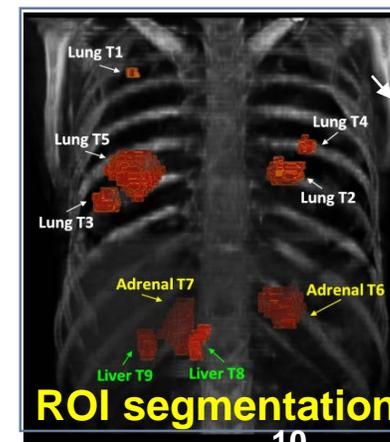
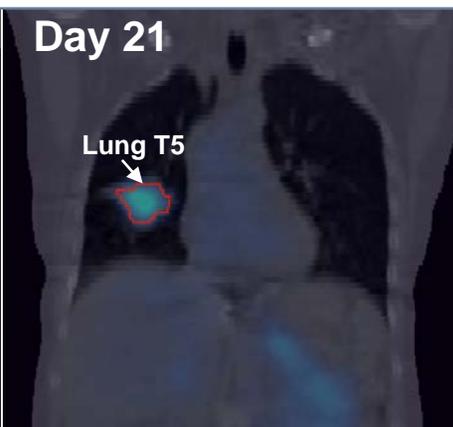
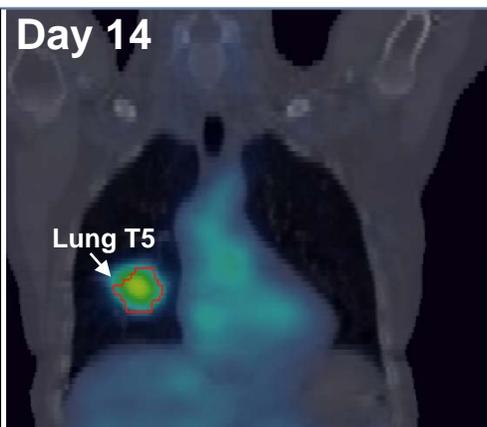
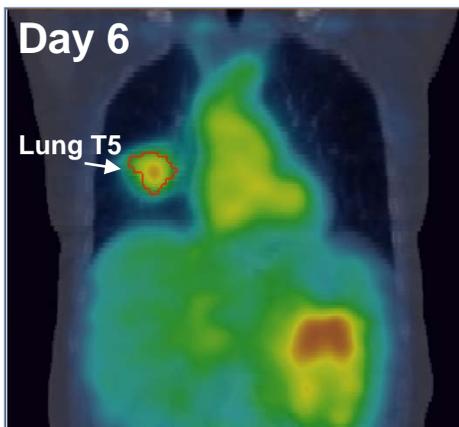


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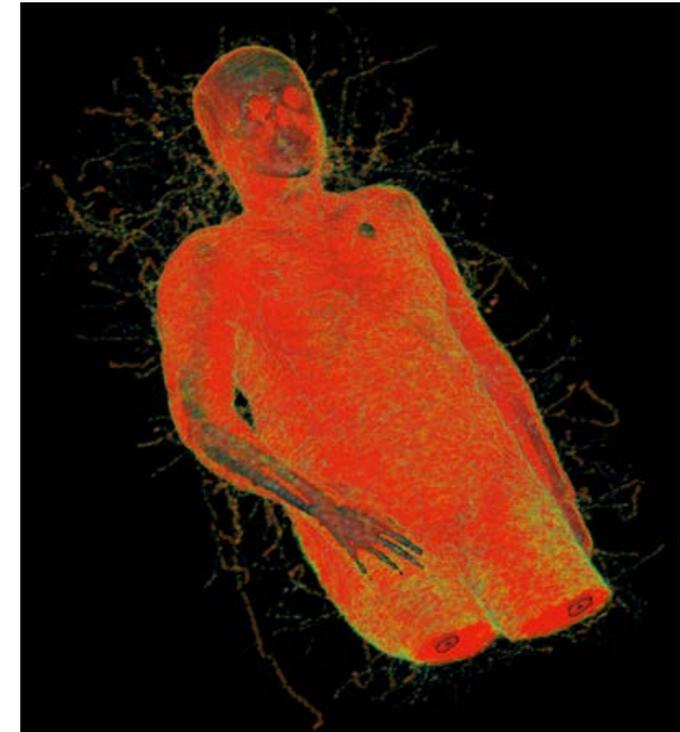
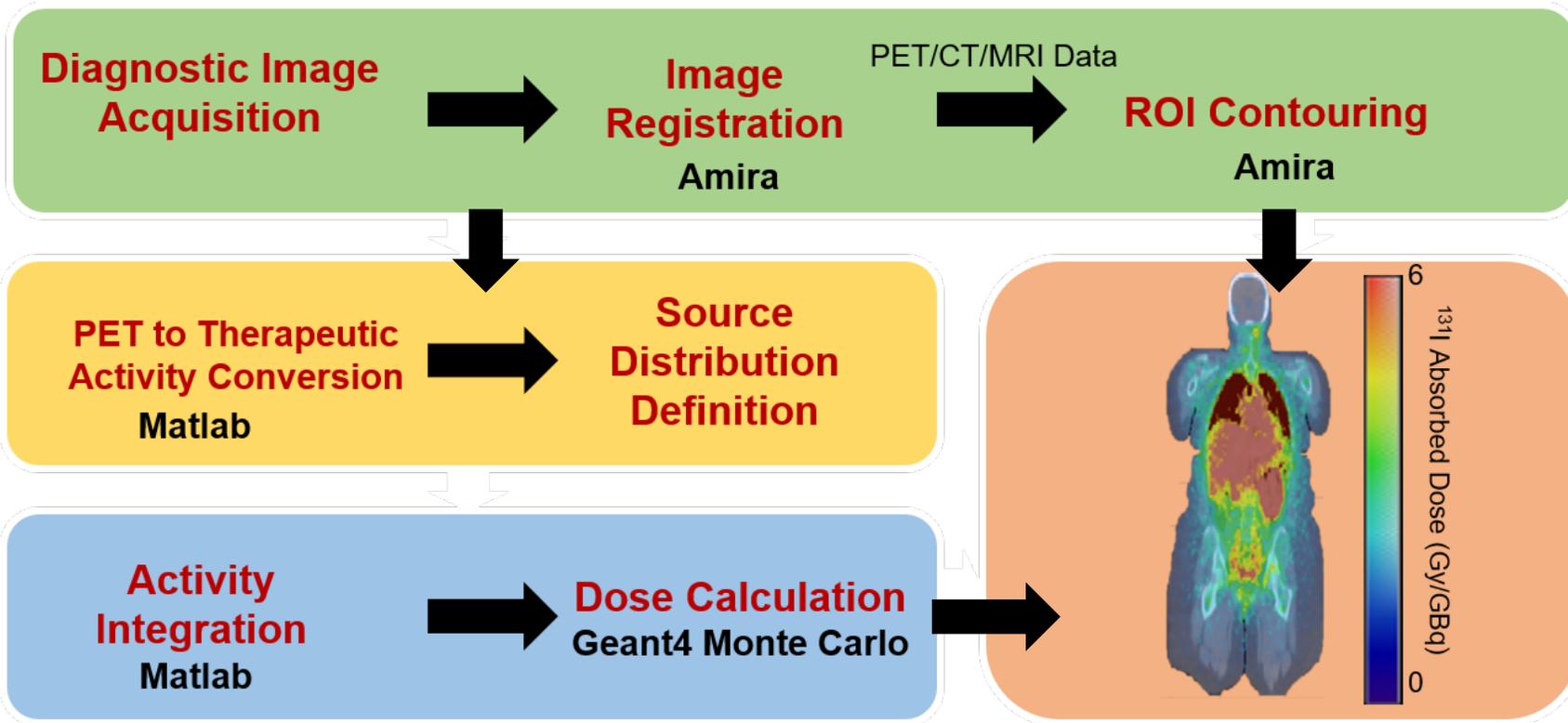
Patient-specific dosimetry can help!

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- **Heterogeneous uptake within the tumor (i.e. heterogeneous dose)**





RAPID (Radiopharmaceutical Assessment Platform for Internal Dosimetry)





No Two Tumors Are Alike

μ PET/CT

SPECT/CT

PET/CT

PDX

Cell Line	No. Mice
NB1691	4
CHLA20	4
Rh30	4
TC71	3
hNET-NB1691	8
TU138	6
SCC22B	4
SCC6	4
SCC2	2
SCC47	2
SCC1483	2
UW1	6
UW13	4
UW64	4
UW22	6
UW25	4
UW36	4
4T1	3
A549	3
B78	12
EL-4	7
HCT116	3
Hut-102	3
LLC	3
MyCap	3
Panco2	3
Colon Adenocarcinoma	3
SCC22B	2

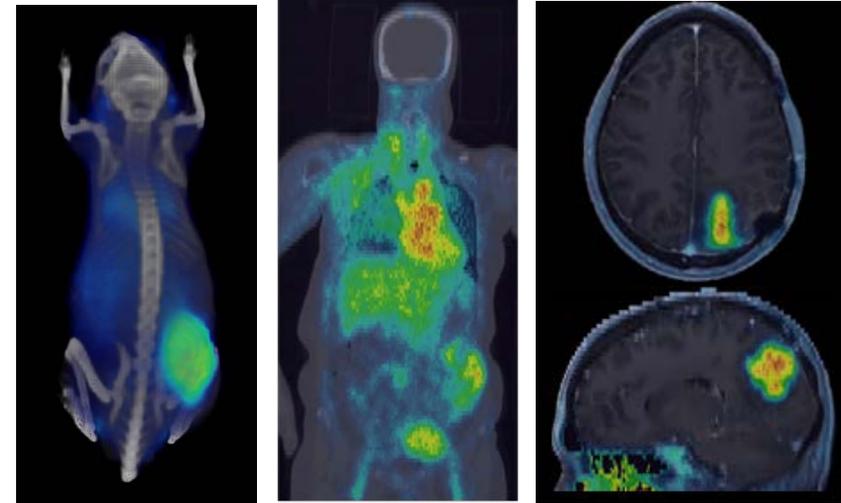
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Cancer Type	No. Tumors
Bone (NonTarget)	1
SCV Node	2
Lung (Left)	
Lung (Right Upper)	9
Lung (Left Lower)	
Lung (Right Lower, NonTarget)	
Lung (Left Ant, NonTarget)	
Lung (Right Additional)	
Adrenal (Left)	
Adrenal (Right)	
Liver (Left)	
Liver (NonTarget)	
Breast (Right)	4
Axial Node (Left, Sup)	
Axial Node (Left, Mid)	
Axial Node (Left, Inf)	
Liver (Center)	3
PeriPortal	
Gastrohepatic Node	

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Cancer Type	No. Tumors
Leiomyosarcoma	1
Rectal	1
Synovial Sarcoma	1
Triple negative breast	1

4

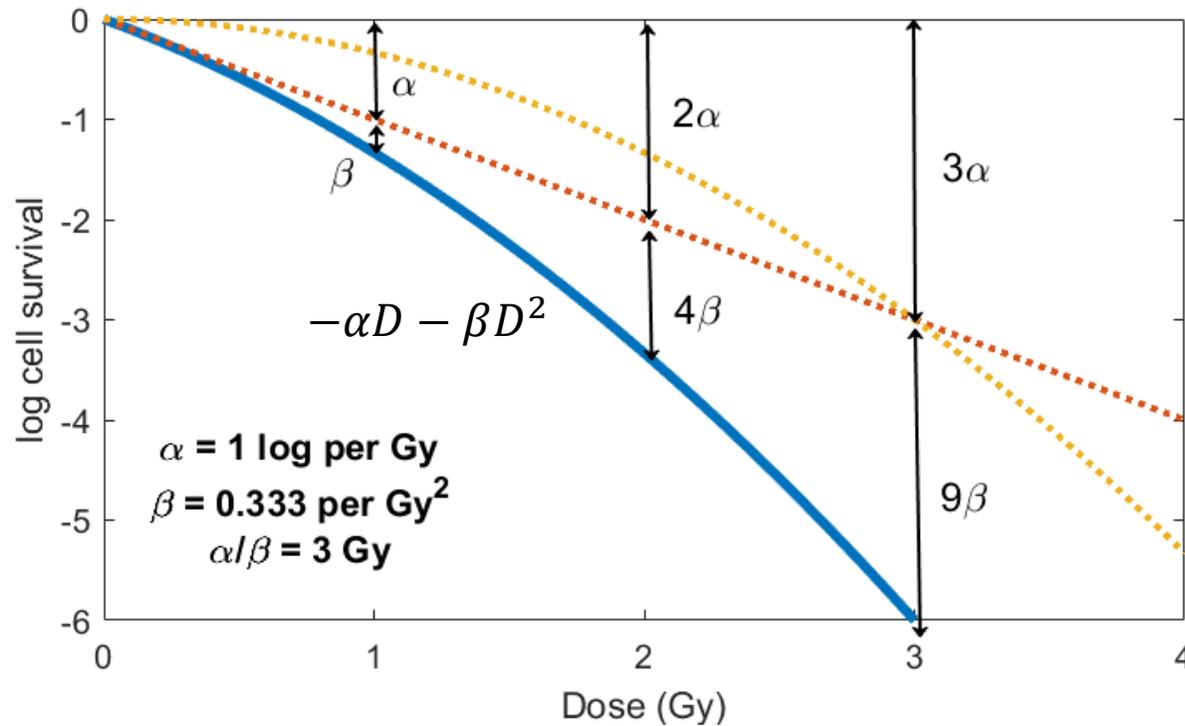


Drug distribution depends on physiological make-up of tumor microenvironment



LQ Model

- The dose of radiation D sterilizes a proportion of cells and the \log_e proportion of surviving cells or cell kill in the exposed population is described by the linear quadratic (LQ) model.



$$\frac{\alpha}{\beta}$$

High: rapidly proliferating tissues
(tumors and early-responders)

Low: slowly proliferating tissues
(late-responders)

α : Intrinsic radiosensitivity (\log_e of number of cells sterilized via non-repairable damage per dose)

β : Repair capacity (\log_e of the number of cells sterilized in a repairable manner per dose-squared)



BED – Biologically Effective Dose

- The radiation dose that would cause the same \log_e cell kill if the dose were delivered with a very small dose rate low enough so that all repairable damage has time to repair.

*Assumes $\dot{d} = \dot{d}_0$

absorbed dose relative effect

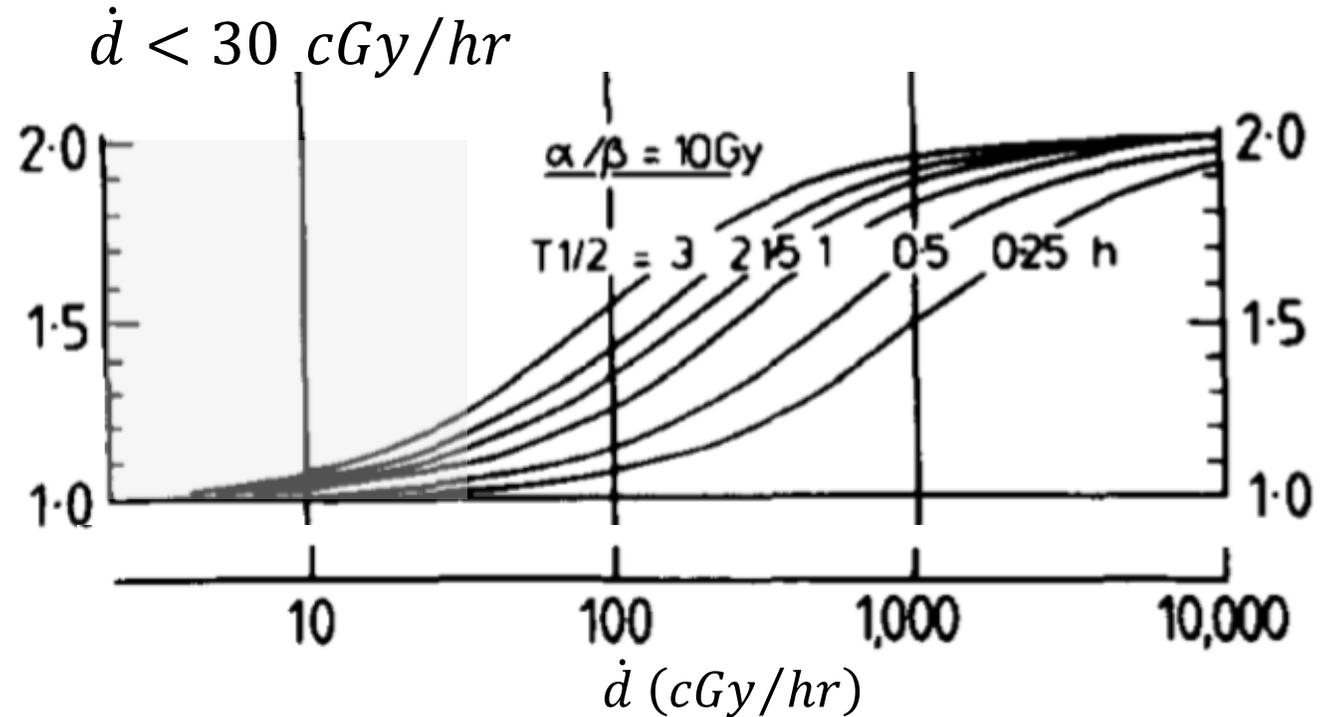
$$BED = D \times RE$$

$$RE = (1 + g\beta D / \alpha)$$

Dose protraction factor*

$$g = \frac{2}{D^2} \int_0^T \dot{d}(t) dt \int_0^t \dot{d}(w) e^{-\mu(t-w)} dw$$

* $g \rightarrow 0$ at low dose rates





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Repopulation rate constant

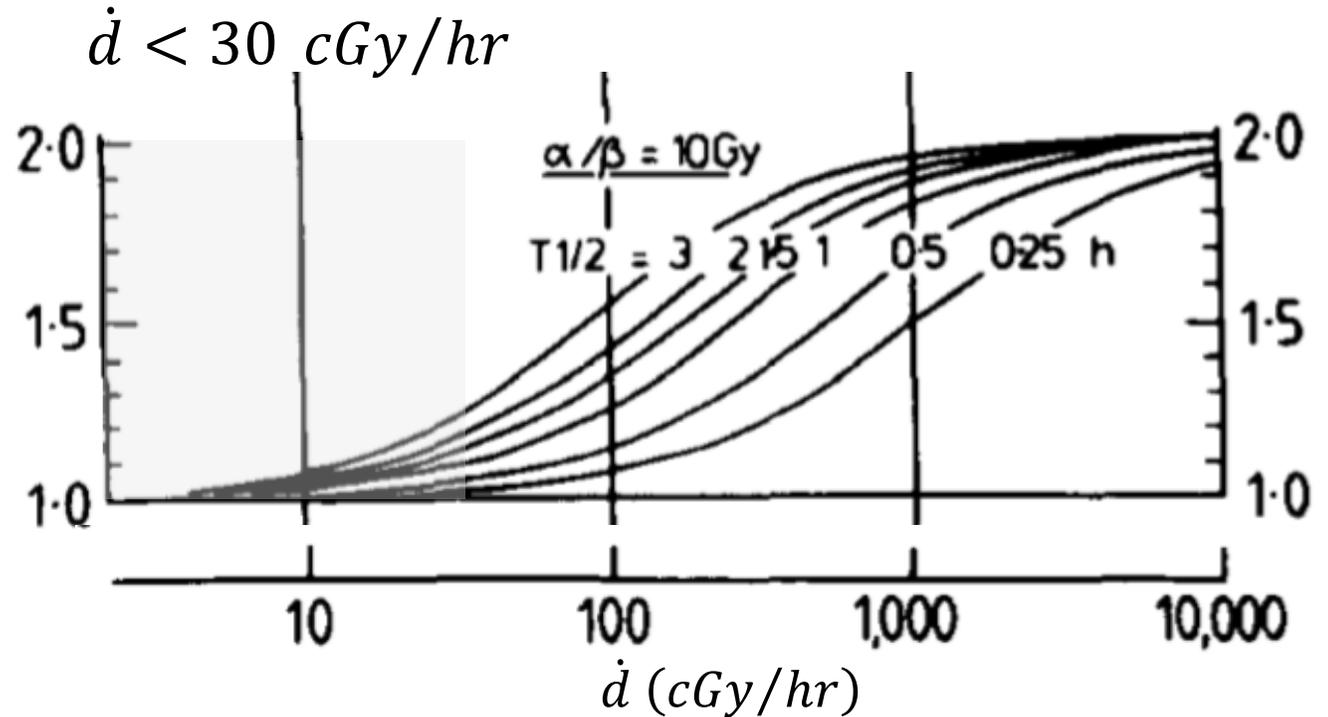
$$BED = D \times RE - (\tau \times t / \alpha)$$

$$RE = (1 + g\beta D / \alpha)$$

Dose protraction factor*

$$g = \frac{2}{D^2} \int_0^T \dot{d}(t) dt \int_0^t \dot{d}(w) e^{-\mu(t-w)} dw$$

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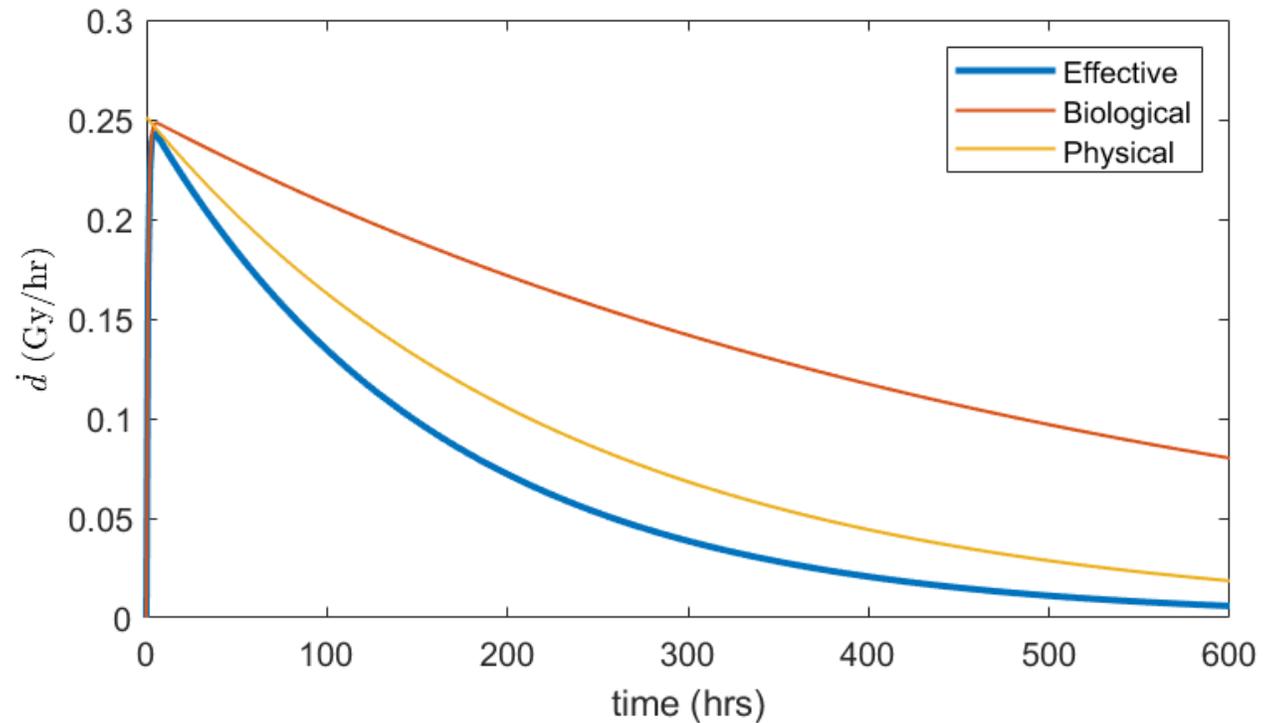
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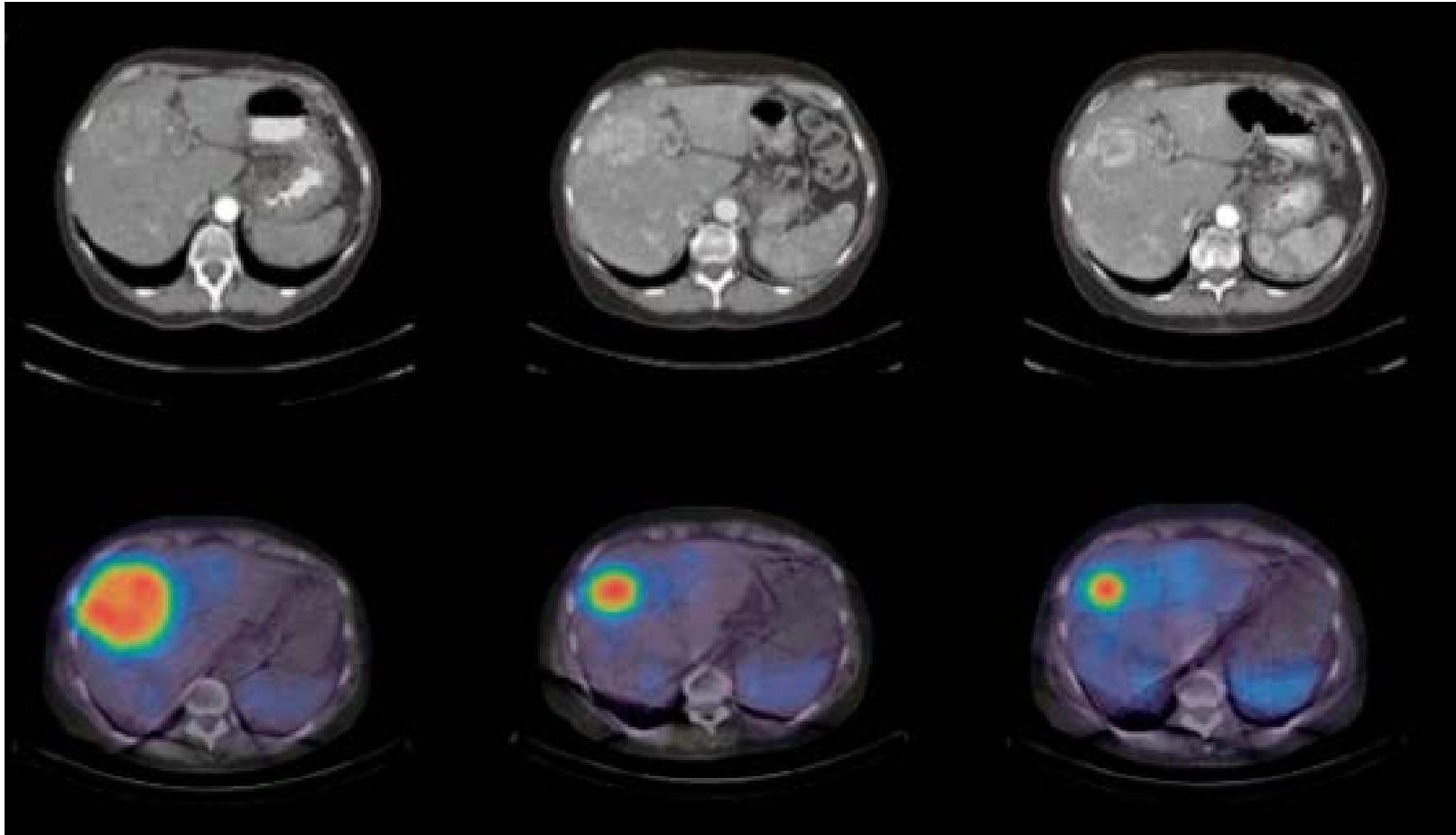
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Tumor Dose Heterogeneity

SPECT/CT of ^{177}Lu -DOTATATE



Ilan et. al JNM, 56(3) 2015



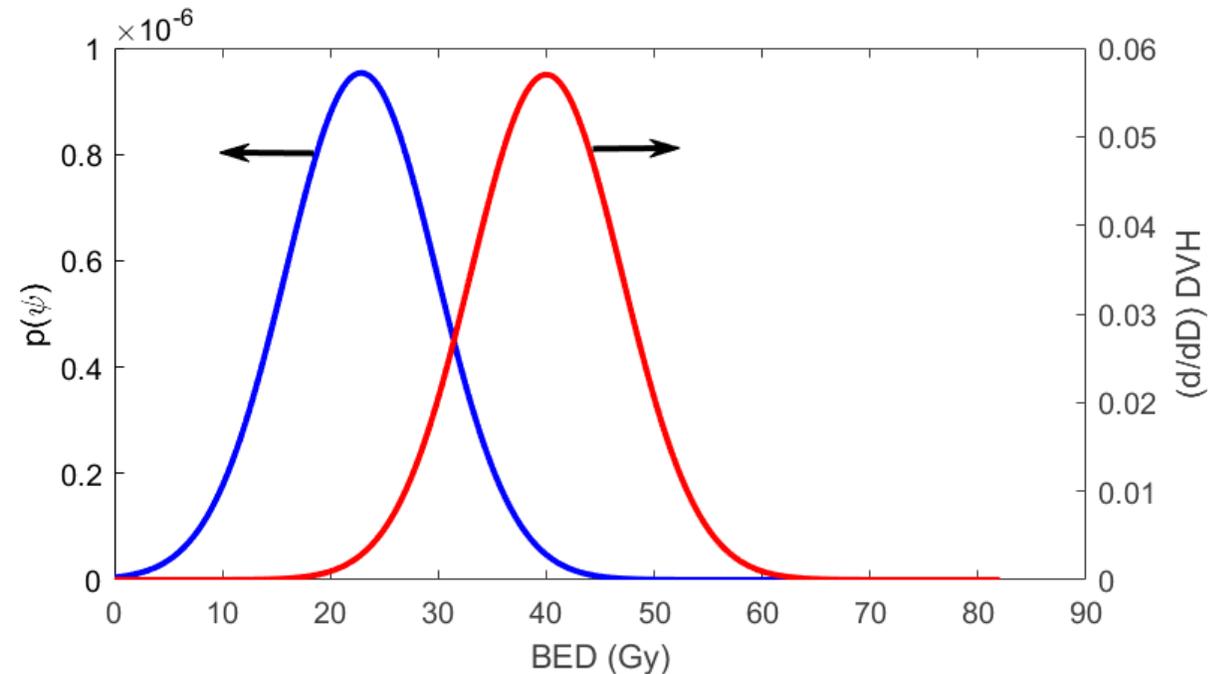
EUD – Equivalent Uniform Dose

- The non-uniform distribution of BED (or dose) that would produce the same \log_e cell kill as the uniform value of BED (or dose)

$$EUD = -\frac{1}{\alpha} \ln(SF(\alpha)) = -\frac{1}{\alpha} \int_0^{\infty} \overbrace{p(\psi) e^{-\alpha\psi}}^{\mathcal{L}(p(\psi))} d\psi$$

where ψ is the BED, $p(\psi)$ is the probability density function of differential DVH with respect to ψ , and:

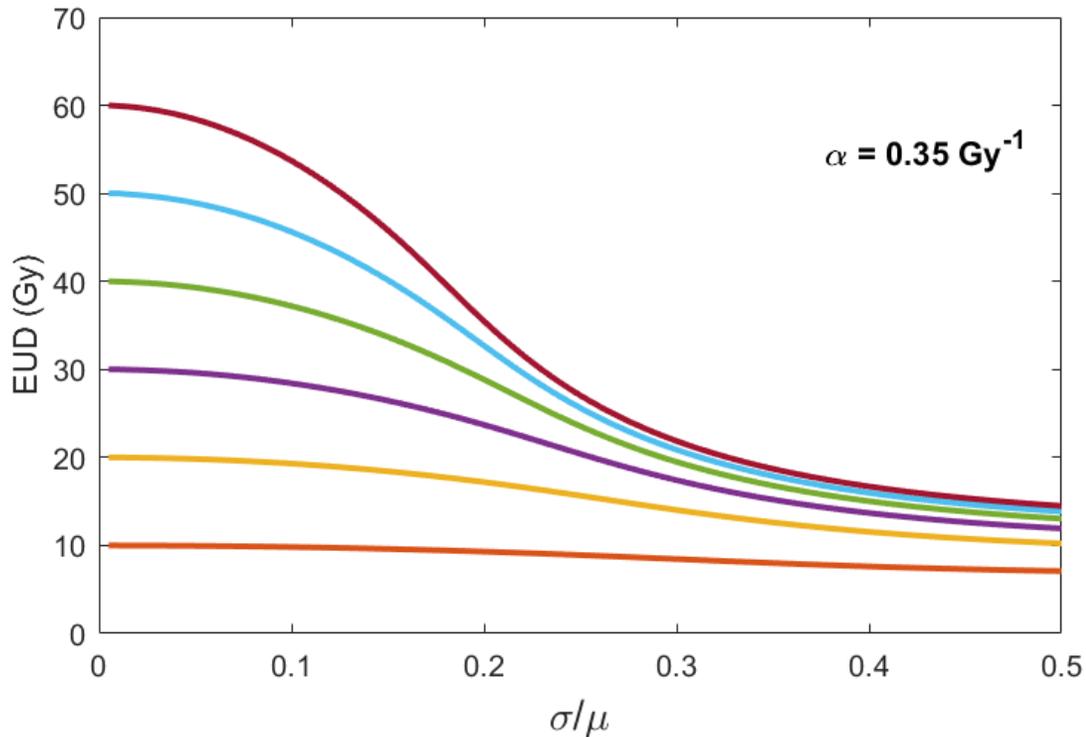
$$SF(\alpha) = \int_0^{\infty} p(\psi) e^{-\alpha\psi} d\psi \rightarrow \text{total survival probability}$$





EUD – Equivalent Uniform Dose

- EUD plotted out as a function of nonuniformity $(\sigma/\mu)^*$



- As the distribution becomes more nonuniform the EUD (hence therapeutic effect) decreases
- The overall loss of therapeutic effectiveness depends on the mean BED and is proportionally worse for greater mean values

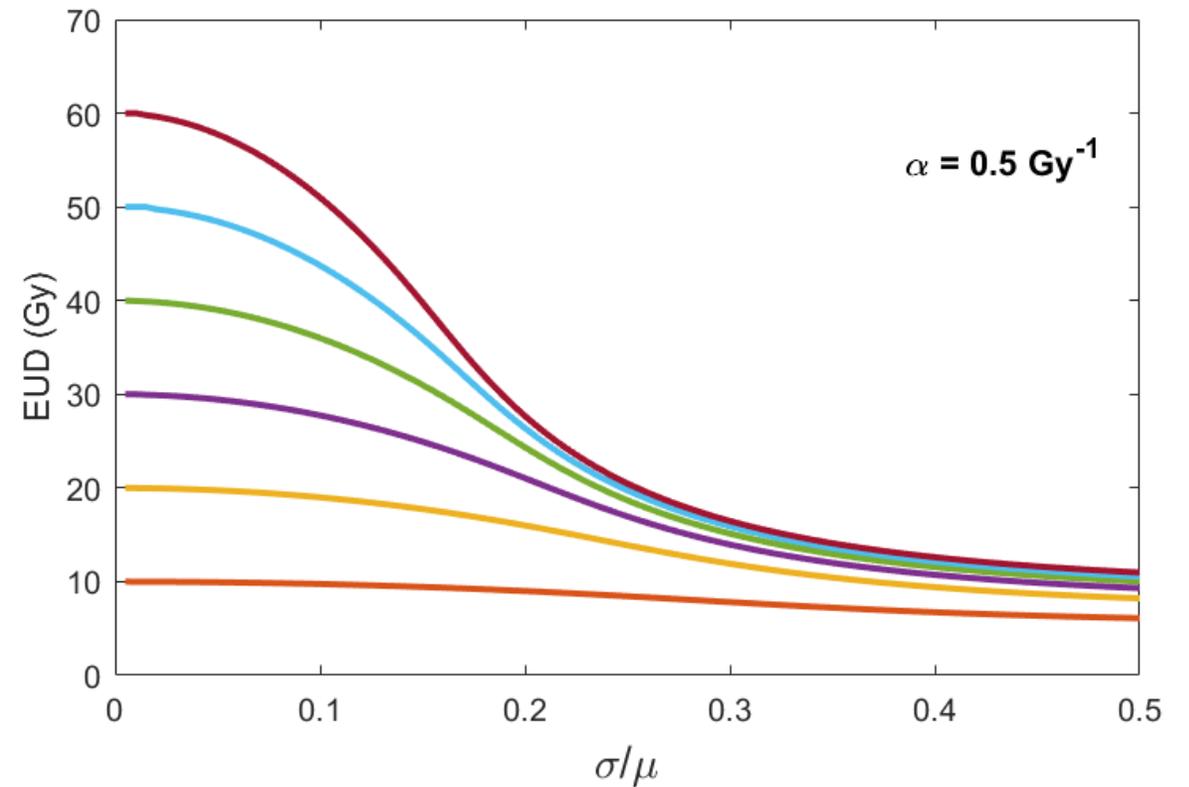
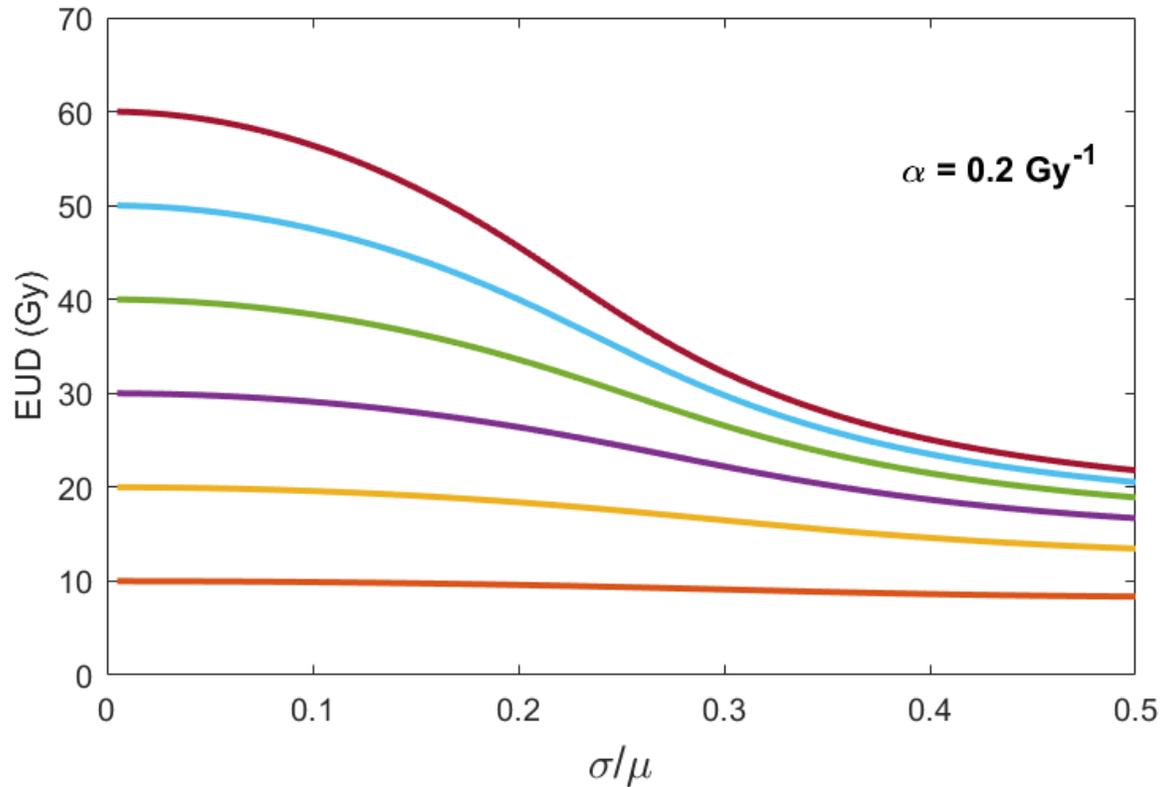
$$\% \text{ Diff}_{60-\text{Gy}} = 76\%$$

$$\% \text{ Diff}_{10-\text{Gy}} = 29\%$$

*assumes dDVH is normally distributed



EUD – Equivalent Uniform Dose



Loss in \log_e cell kill is proportionally worse for radiosensitive tumors

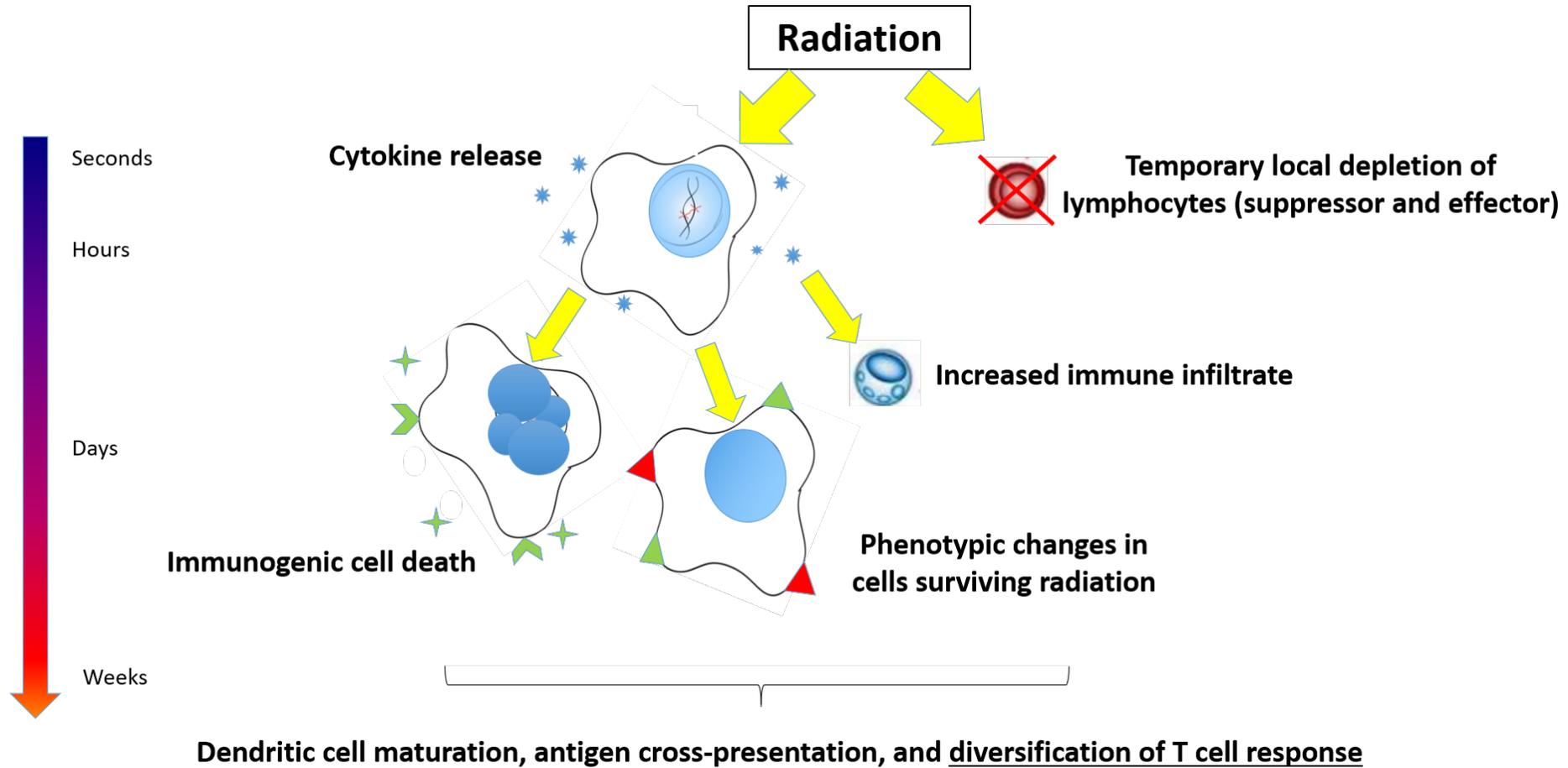


Discussion Points

- Models such as LQ that reflect the biological effect of the RPT agent on tumor (and normal) cells should be more meaningful than absorbed dose.
- Despite several efforts correlations between BED or EUD and effect have been difficult to detect.
- New models that better reflect the tumor microenvironment should be investigated.



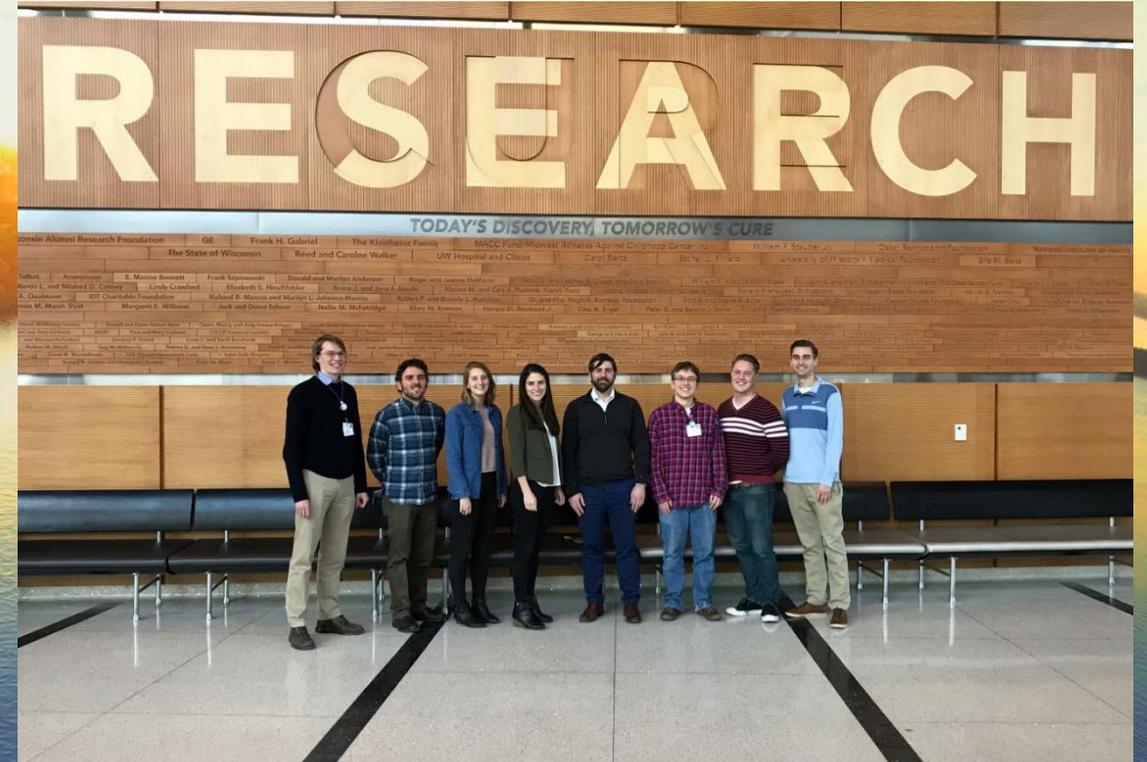
Discussion Points



Acknowledgements

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Bryan P. Bednarz, Ph.D.
Associate Professor
Department of Medical Physics
University of Wisconsin-Madison
1111 Highland Ave., L5-176
Madison, WI 53705-2275
o - (608) 262-5225
c - (734) 678-2346
bbednarz2@wisc.edu



Thank You!